

**KENDRIYA VIDYALAYA SANGATHAN, HYDERABAD REGION**  
**SAMPLE PAPER 01 FOR HALF YEARLY EXAM (2017-18)**

**SUBJECT: MATHEMATICS**

**MAX. MARKS : 80**

**CLASS : X**

**DURATION : 3 HRS**

**General Instructions:**

- (i). All questions are compulsory.
- (ii). This question paper contains **30** questions divided into four Sections A, B, C and D.
- (iii). **Section A** comprises of 6 questions of **1 mark** each. **Section B** comprises of 6 questions of **2 marks** each. **Section C** comprises of 10 questions of **3 marks** each and **Section D** comprises of 8 questions of **4 marks** each.
- (iv). Use of Calculators is not permitted

**SECTION – A**

1. If the sum of the zeroes of the polynomial  $f(x) = 2x^3 - 3kx^2 + 4x - 5$  is 6, then find the value of  $k$ .
2. State Euclid's division lemma
3. Find the value of  $k$  for which the system of equations  $x - 2y = 3$  and  $3x + ky = 1$  has a unique solution.
4. If  $\triangle ABC \sim \triangle PQR$ ,  $BC = 8$  cm and  $QR = 6$  cm, find the ratio of the areas of  $\triangle ABC$  and  $\triangle PQR$ .
5. If  $2x$ ,  $x + 10$ ,  $3x + 2$  are in A.P., find the value of  $x$ .
6. If  $\sin A = \frac{1}{2}$ , find the value of  $\frac{2 \sec A}{1 + \tan^2 A}$ .

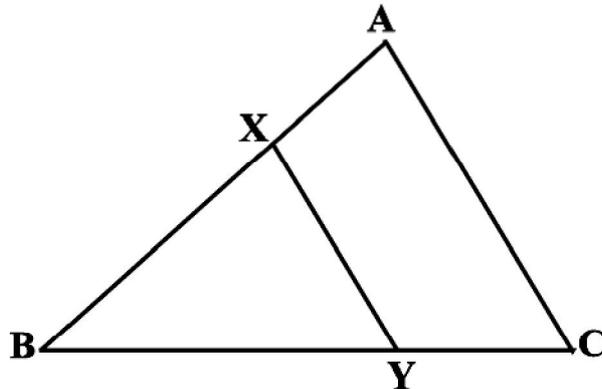
**SECTION – B**

7. Using Euclid's division algorithm, find the HCF of 2160 and 3520.
8. If  $\sec A + \tan A = m$  and  $\sec A - \tan A = n$ , find the value of  $\sqrt{mn}$ .
9. If  $A$  and  $B$  are angles of right angled triangle  $ABC$ , right angled at  $C$ , prove that  $\sin^2 A + \sin^2 B = 1$
10. Find the zeroes of the quadratic polynomial  $5t^2 + 12t + 7$  and verify the relationship between the zeroes and the coefficients.
11. Find the value of  $k$  if the points  $A(2, 3)$ ,  $B(4, k)$  and  $C(6, -3)$  are collinear.
12. Find the roots of  $\frac{1}{x} - \frac{1}{x-2} = 3, x \neq 0, 2$

**SECTION – C**

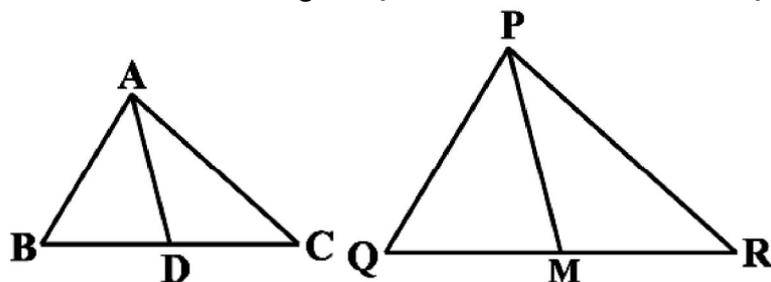
13. Find the quotient and remainder when  $4x^3 + 2x^2 + 5x - 6$  is divided by  $2x^2 + 3x + 1$ .
14. Solve  $2x + 3y = 11$  and  $2x - 4y = -24$  and hence find the value of ' $m$ ' for which  $y = mx + 3$ .

15. Prove that  $\sqrt{5}$  is an irrational number.
16. Show that the square of an odd positive integer can be of the form  $6q + 1$  or  $6q + 3$  for some integer  $q$ .
17. If  $(1, 2)$ ,  $(4, y)$ ,  $(x, 6)$  and  $(3, 5)$  are the vertices of a parallelogram taken in order, find  $x$  and  $y$ .
18. Find the ratio in which the line segment joining the points  $(-3, 10)$  and  $(6, -8)$  is divided by  $(-1, 6)$ .
19. If the sum of the first 14 terms of an AP is 1050 and its first term is 10, find the 20th term.
20. Find the roots of the equation  $5x^2 - 6x - 2 = 0$ , by method of completing the square.
21. Prove that:  $\frac{1}{\operatorname{cosec} A - \cot A} - \frac{1}{\sin A} = \frac{1}{\sin A} - \frac{1}{\operatorname{cosec} A + \cot A}$ .
22. In the below figure, the line segment  $XY$  is parallel to side  $AC$  of  $\Delta ABC$  and it divides the triangle into two parts of equal areas. Find the ratio  $\frac{AX}{AB}$ .



**SECTION – D**

23. Prove that “The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.”
24. Sides  $AB$  and  $AC$  and median  $AD$  of a triangle  $ABC$  are respectively proportional to sides  $PQ$  and  $PR$  and median  $PM$  of another triangle  $PQR$ . Show that  $\Delta ABC \sim \Delta PQR$ .



25. Places  $A$  and  $B$  are 100 km apart on a highway. One car starts from  $A$  and another from  $B$  at the same time. If the cars travel in the same direction at different speeds, they meet in 5 hours. If they travel towards each other, they meet in 1 hour. What are the speeds of the two cars? While driving, the driver should maintain the speed limit as allowed. Comment